

# On Vague Ordered Gamma-Near Rings

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## Article Info

Volume 83

Page Number: 6740 - 6745

Publication Issue:

March - April 2020

## Abstract:

Abstract: In this paper, we originate and inspect the notion of vague Ordered  $\Gamma$ -Near rings and its properties. We establish one-one correspondence between Vague Ordered  $\Gamma$ -Near ring and crisp Ordered  $\Gamma$ -Near ring. Also, we provide the necessary and sufficient condition for a vague set to be a vague ordered  $\Gamma$ -Near ring.

## Article History

Article Received: 24 July 2019

Revised: 12 September 2019

Accepted: 15 February 2020

Publication: 05 April 2020

**Keywords:** Vague set, Vague Ordered  $\Gamma$ -Near ring

## I. INTRODUCTION

The hypothesis of fuzzy Near rings has been created by Bh. Satyanarayana [1] and G.L. Booth. Afterward W.L. Gau and D.J. Buehrer [18] presented the hypothesis of vague sets as an improvement of the hypothesis of fuzzy sets in resembling the valid condition. Vague sets are higher classification of fuzzy sets. As per them a vague set  $A$  in the universe of discourse  $U$  is a pair  $(t_A, f_A)$ , where  $t_A$  and  $f_A$  are fuzzy subsets of  $U$  fulfilling  $t_A(u) + f_A(u) \leq 1, \forall u \in U$ .

Further K. Balakoteswara Rao [2] had introduced and studied the concepts of  $L$ -Fuzzy sub Ordered  $\Gamma$ -Near ring. As an overview of it, we introduce the algebraic structure "vague Ordered  $\Gamma$ -Near rings (VOG NR)". We establish one-one correspondence between VOG NR and crisp OG NR. We confirm that the intersection of two VOG NRs is also VOG NR.

## II. PRELIMINARIES

Definition 2.1 : A zero - symmetric GNR is a triple  $(\tilde{K}, +, \Gamma)$ , where

1.  $(\tilde{K}, +)$  is a group
2.  $(\tilde{K}, +, \delta)$  is a nearring where  $\Gamma \neq \Phi$  with binary operators on  $\tilde{K}$ ,  $\forall \delta \in \Gamma$ .
3.  $f \delta (g \eta h) = (f \delta g) \eta h \quad \forall f, g, h \in \tilde{K}; \delta, \eta \in \Gamma$ .
4.  $f \delta g = 0, \forall f \in \tilde{K}, \delta \in \Gamma$ .

Definition 2.2 :  $E \neq \Phi, A \subseteq \tilde{K}$ , where  $\tilde{K}$  be a GNR is said to be a SGNR if

1.  $f - g \in E$
2.  $f \delta g \in E, \forall \delta \in \Gamma; f, g \in \tilde{K}$

Definition 2.3: A Fuzzy subset  $W$  of  $\tilde{K}$  is a Fuzzy SGNR, if

1.  $W(f - g) \geq \{W(f), W(g)\}$
2.  $W(f \delta g) \geq \{W(f), W(g)\}, \forall \delta \in \Gamma; f, g \in \tilde{K}$

Definition 2.4 : The vague value of  $w$  in  $N = (t_N, f_N)$  is defined as  $V_N(w) = [t_N(w), 1 - f_N(w)]$ .

Definition 2.5 : The union of two vague sets  $N$  and  $M$  is defined as

$$t_C = \max \{t_N, t_M\}; \\ 1 - f_C = \{1 - f_N, 1 - f_M\}.$$

Definition 2.6 : The intersection of two vague sets  $N$  and  $M$  is defined as

$$t_C = \min \{t_N, t_M\}; 1 - f_C = \{1 - f_N, 1 - f_M\}.$$

Definition 2.7 : The vague-cut of a vague set  $N$  is the crisp subset of  $U$  is given by

$$N_{(\beta, \gamma)} = \{f \in U; V_N \geq [\beta, \gamma]\}.$$

Definition 2.8 : A vague set  $N = (t_N, f_N)$  of  $\tilde{K}$  is called as a VGNR if

1.  $V_N(f - g) \geq \{V_N(f), V_N(g)\}$
2.  $V_N(f \delta g) \geq \{V_N(f), V_N(g)\};$   
 $\forall \delta \in \Gamma; f, g \in \tilde{K}$

Definition 2.9 : A GNR,  $\tilde{K}$  is called as an OGNR if it admits a compatible relation " $\leq$ ", If  $a \leq b$  and  $c \leq d$  then

1.  $a + c \leq b + d$
2.  $a\delta c \leq b\delta d$
3.  $c\delta a \leq d\delta b; \forall a, b, c, d \in \tilde{K}; \delta \in \Gamma.$

Definition 2.10 : Let  $\tilde{K}$  be a partially OGNR.  $\emptyset \neq N$  of  $\tilde{K}$  is said to be SOGNR, if

1.  $f - g \in N$
2.  $f\delta g \in N$
3. if  $a \leq b$  then  $a + f \leq b + g$
4. if  $a \leq b$  and  $c \geq 0$  then  $c\delta a \leq c\delta b$  and  $a\delta c \leq b\delta c;$   
 $\forall a, b, c, f, g \in \tilde{K}; \delta \in \Gamma.$

Definition 2.11 : Let  $\tilde{K}$  be an OGNR. A fuzzy subset  $W$  of  $\tilde{K}$  is said to be FSOGNR of  $\tilde{K}$  if

1.  $W(f - g) \geq \{W(f), W(g)\}$
2.  $W(f \delta g) \geq \{W(f), W(g)\},$
3.  $f \leq g \Rightarrow W(f) \geq W(g); \forall \delta \in \Gamma;$   
 $f, g \in \tilde{K}.$

#### Notations :

1.  $\tilde{K}$  stands for Zero – Symmetric Ordered  $\Gamma$  – Near ring.
2. OGNR stands for Ordered  $\Gamma$  – Near ring.
3. GNR stands for  $\Gamma$  – Near ring.
4. SGNR stands for Sub  $\Gamma$  – Near ring.
5. VGNR stands for Vague  $\Gamma$  – Near ring.
6. FSOGNR stands for Fuzzy Sub Ordered

$\Gamma$  – Near ring.

7. VOGNR stands for Vague Ordered  $\Gamma$  – Near ring.

8. FOGNR stands for Fuzzy Ordered  $\Gamma$  – Near ring.

### III. MAIN RESULTS

Definition 3.1 : A vague set  $N = (t_N, f_N)$  of  $\tilde{K}$  is said to be VOGNR if

1.  $V_N(f - g) \geq \{V_N(f), V_N(g)\}$
2.  $V_N(f \delta g) \geq \{V_N(f), V_N(g)\}$
3.  $f \leq g \Rightarrow V_N(f) \geq V_N(g); \forall \delta \in \Gamma; f, g \in \tilde{K}$

i.e.,

1.  $t_N(f - g) \geq \{t_N(f), t_N(g)\}$
2.  $t_N(f \delta g) \geq \{t_N(f), t_N(g)\}$
3.  $f \leq g \Rightarrow t_N(f) \geq t_N(g); \forall \delta \in \Gamma; f, g \in \tilde{K}$  and

1.  $1 - f_N(f - g) \geq \{1 - f_N(f), 1 - f_N(g)\}$
2.  $1 - f_N(f \delta g) \geq \{1 - f_N(f), 1 - f_N(g)\}$
3.  $f \leq g \Rightarrow 1 - f_N(f) \geq 1 - f_N(g);$   
 $\forall \delta \in \Gamma; f, g \in \tilde{K}$

Example 3.2 : Let  $\tilde{K} = \Gamma = "z"$  ( the set of integers) which is clearly a GNR. Also, "z" admits a compatible relation " $\leq$ " which is a partial ordering on  $\tilde{K}$ .

Hence  $\tilde{K}$  is an OGNR. Let  $N = (t_N, f_N)$ , where  $t_N: \tilde{K} \rightarrow [0,1], f_N: \tilde{K} \rightarrow [0,1]$   
Defined by

$$\begin{aligned} t_N(f) &= \{0.3, \quad \text{if } f \\ &= 0.4, \text{ if } f \text{ is positive } 0.6, \text{ if } f \text{ is negative} \\ t_N(f) &= \{0.7, \quad \text{if } f \\ &= 0.5, \text{ if } f \text{ is positive } 0.4, \text{ if } f \text{ is negative} \end{aligned}$$

Then  $N$  is a VOGNR of  $\tilde{K}$ .

**Theorem 3.3 :** A necessary and sufficient condition for a vague set  $N = (t_N, f_N)$ , of  $\tilde{K}$  to be a VOGNR of  $\tilde{K}$  is that  $t_N$  and  $1 - f_N$  are FOGNRs of  $\tilde{K}$ .

Proof : Suppose  $N = (t_N, f_N)$ , is a VOGNR of  $\tilde{K}$ .

$$\text{Let } \forall \delta \in \Gamma; f, g \in \tilde{K}. \text{ Then } V_N(f - g) \geq \{V_N(f), V_N(g)\}$$

$$V_N(f \delta g) \geq \{ V_N(f), V_N(g) \}$$

$$f \leq g \Rightarrow V_N(f) \geq V_N(g); \forall \delta \in \Gamma; f, g \in \tilde{K}$$

i.e.,

$$t_N(f - g) \geq \{ t_N(f), t_N(g) \}$$

$$t_N(f \delta g) \geq \{ t_N(f), t_N(g) \}$$

$$f \leq g \Rightarrow t_N(f) \geq t_N(g); \forall \delta \in \Gamma; f, g \in \tilde{K}$$

and

$$1 - f_N(f - g) \geq \{ 1 - f_N(f), 1 - f_N(g) \}$$

$$1 - f_N(f \delta g) \geq \{ 1 - f_N(f), 1 - f_N(g) \}$$

$$f \leq g \Rightarrow 1 - f_N(f) \geq 1 - f_N(g);$$

Hence  $t_N$  and  $1 - f_N$  are FOGNR of M. The converse part is clear from the definition.

**Theorem 3.4 :** A vague set  $N = (t_N, f_N)$  of M is a VOGNR of M if and only if for any  $\beta, \gamma \in [0,1]$  the vague cut  $N_{(\beta, \gamma)}$  is a SOGNR of M.

Proof: Suppose  $N$  is a VOGNR of  $\tilde{K}$ .

Let  $f, g \in N_{(\beta, \gamma)}$  and  $\delta \in \Gamma$ .

$$V_N(f) \geq [\beta, \gamma] \text{ and } V_N(g) \geq [\beta, \gamma]$$

We have

$$V_N(f - g) \geq \{ V_N(f), V_N(g) \} \geq [\beta, \gamma]$$

$$\Rightarrow f - g \in N_{(\beta, \gamma)}$$

$$V_N(f \delta g) \geq \{ V_N(f), V_N(g) \} \geq [\beta, \gamma]$$

$$\Rightarrow f \delta g \in N_{(\beta, \gamma)}$$

Clearly  $N_{(\beta, \gamma)}$  admits partial ordering.

Hence  $N_{(\beta, \gamma)}$  is SOGNR of  $\tilde{K}$ .

Conversely suppose  $N_{(\beta, \gamma)}$  is SOGNR of  $\tilde{K}$ .

$$[\beta, \gamma] = \min\{[\beta_1, \gamma_1], [\beta_2, \gamma_2]\}$$

$$\text{Then } f, g \in N_{(\beta, \gamma)} \Rightarrow f - g \in N_{(\beta, \gamma)}$$

$$\text{And } f \delta g \in N_{(\beta, \gamma)}$$

$$\text{Which implies } V_N(f - g) \geq \{ V_N(f), V_N(g) \}$$

$$\text{And } V_N(f \delta g) \geq \{ V_N(f), V_N(g) \}$$

$$\text{Let } f \leq g, \text{ suppose if possible } V_N(f) < V_N(g)$$

$$[\beta_1, \gamma_1] \in [0,1]$$

$$V_N(f) < [\beta_1, \gamma_1] < V_N(g)$$

$$g \in N_{([\beta_1, \gamma_1])} \text{ and } f \notin N_{([\beta_1, \gamma_1])}$$

which is a contradiction.

$$\text{Therefore } V_N(f) \geq V_N(g).$$

Hence  $N$  is VOGNR of  $\tilde{K}$ .

**Corollary 3.5 :** Let  $N$  be a VOGNR of  $\tilde{K}$ . Then for  $\beta \in [0,1]$ , the  $\beta$  cut  $N_\beta$  is a SOGNR of  $\tilde{K}$ .

Now, we introduce the vague characteristic set of  $\tilde{K}$ .

**Definition 3.6 :** Let characteristic set  $\chi = (t_\chi, f_\chi)$  be a vague set of  $\tilde{K}$ . For any subset  $S$  of  $\tilde{K}$ , the vague characteristic set of  $S$  taking values in  $[0,1]$  is defined by

$$V_{\chi_s}(f) = \{ [1,1] \text{ if } f \in S, [0,0] \text{ if } f \notin S \}$$

Then  $\chi_s$  is called the vague characteristic set of  $S$  in  $[0,1]$ .

**Theorem 3.7 :** Let  $\emptyset \neq S \subseteq \tilde{K}$ . Then the vague characteristic set  $V_{\chi_s}$  of ' $S$ ' is VOGNR of  $\tilde{K}$  if and only if ' $S$ ' is SOGNR of  $\tilde{K}$ .

Proof: Suppose  $\chi_s$  is a VOGNR of  $\tilde{K}$ .

Let  $\forall \delta \in \Gamma; f, g \in S$ . Then

$$V_{\chi_s}(f - g) \geq \{ V_{\chi_s}(f), V_{\chi_s}(g) \} = [1,1]$$

$$\Rightarrow f - g \in S$$

$$V_{\chi_s}(f \delta g) \geq \{ V_{\chi_s}(f), V_{\chi_s}(g) \} = [1,1]$$

$$\Rightarrow f \delta g \in S$$

Since  $S \subseteq \tilde{K}$ , it admits partial ordering

$$f \leq g \Rightarrow V_{\chi_s}(f) \geq V_{\chi_s}(g);$$

Thus ' $S$ ' is SOGNR of  $\tilde{K}$ .

Suppose ' $S$ ' is SOGNR of  $\tilde{K}$ .

Let  $f, g \in \tilde{K}$  and  $\forall \delta \in \Gamma$

If  $f, g \in S \Rightarrow f - g \in S, f \delta g \in S$  then

$$V_{\chi_s}(f - g) = [1,1] = \{ V_{\chi_s}(f), V_{\chi_s}(g) \}$$

$$V_{\chi_s}(f \delta g) = [1,1] = \{ V_{\chi_s}(f), V_{\chi_s}(g) \}$$

If  $f, g \notin S \Rightarrow f - g \notin S, f \delta g \notin S$  then

$$V_{\chi_s}(f - g) = [0,0] = \{ V_{\chi_s}(f), V_{\chi_s}(g) \}$$

$$V_{\chi_s}(f \delta g) = [0,0] = \{ V_{\chi_s}(f), V_{\chi_s}(g) \}$$

A similar argument can be made if  $f \in S$  and  $g \notin S$ .

For  $f \leq g$

If  $f, g \in S$  then  $V_{\chi_s}(f) = [1,1]$  and  $V_{\chi_s}(g) = [1,1]$  implies  $V_{\chi_s}(f) \geq V_{\chi_s}(g)$

If  $f, g \notin S$  then  $V_{\chi_s}(f) = [0,0]$  and

$$V_{\chi_s}(g) = [0,0] \text{ implies } V_{\chi_s}(f) \geq V_{\chi_s}(g)$$

If  $f \in S$  and  $g \notin S$  then  $V_{\chi_s}(f) = [1,1]$  and

$$V_{\chi_s}(g) = [0,0] \text{ implies } V_{\chi_s}(f) \geq V_{\chi_s}(g)$$

Thus  $\chi_s$  is a VOGNR of  $\tilde{K}$ .

**Theorem 3.8 :**

Let  $S$  be a SOGNR of  $\tilde{K}$ . Then for any

$0 < \beta < \gamma < 1, \exists$  VOGNR,  $N$  of  $\tilde{K}$ ;

$\exists, N_{(\beta, \gamma)} = S$ .

Proof : Let  $S$  be a SOGMR of a GMR  $\tilde{K}$ .

Define a vague set  $N = (t_N, f_N)$  on  $\tilde{K}$  by

$$V_N(f) = \{[\beta, \gamma] \mid f \in S [0, 0] \mid f \notin S\}$$

Clearly,  $N_{(\beta, \gamma)} = N$ .

If  $f, g \in \tilde{K} ; \forall \delta \in \Gamma \Rightarrow f - g \in \tilde{K}, f \delta g \in \tilde{K}$  then

$$V_N(f - g) = [\beta, \gamma] = \{V_N(f), V_N(g)\}$$

$$V_N(f \delta g) = [\beta, \gamma] = \{V_N(f), V_N(g)\}$$

If  $f, g \notin \tilde{K}$  then

$$V_N(f - g) = [0, 0] = \{V_N(f), V_N(g)\}$$

$$V_N(f \delta g) = [0, 0] = \{V_N(f), V_N(g)\}$$

if  $f \notin S$  and  $g \in S$  then  $V_N(f) =$

$$[0, 0] \text{ and } V_N(g) = [\beta, \gamma]$$

$$V_N(f - g) \geq \{V_N(f), V_N(g)\}$$

$$V_N(f \delta g) \geq \{V_N(f), V_N(g)\}$$

A similar argument could be made for  $f \in S$  and  $g \notin S$ .

For  $f \leq g$

If  $f, g \in S$  then  $V_N(f) = [\beta, \gamma]$  and

$$V_N(g) = [\beta, \gamma] \Rightarrow V_N(f) \geq V_N(g)$$

If  $f, g \notin S$  then  $V_N(f) = [0, 0]$  and

$$V_N(g) = [0, 0] \Rightarrow V_N(f) \geq V_N(g)$$

If  $f \in S$  and  $g \notin S$  then  $V_N(f) = [\beta, \gamma]$  and

$$V_N(g) = [0, 0] \Rightarrow V_N(f) \geq V_N(g)$$

Hence,  $N_{(\beta, \gamma)} = S$ .

**Theorem 3.9 :** Let  $N = (t_N, f_N)$  be a VOGMR of a left (resp, right) zero OGNR  $\tilde{K}$ .

Then  $V_N(f) = V_N(g), \forall f, g \in \tilde{K}$ .

Proof : Let  $\tilde{K}$  be a left zero OGNR.

Let  $f, g \in \tilde{K} ; \forall \delta \in \Gamma$ .

Since  $\tilde{K}$  is left zero  $\Rightarrow f \delta g = f$  and  $g \delta f = g$ .

Now,

$$\begin{aligned} V_N(f \delta g) &\geq \{V_N(f), V_N(g)\} \\ &\Rightarrow V_N(f) \geq \{V_N(f), V_N(g)\} \\ &\Rightarrow V_N(f) \geq V_N(g) \end{aligned}$$

Also,

$$\begin{aligned} V_N(g \delta f) &\geq \{V_N(f), V_N(g)\} \\ &\Rightarrow V_N(g) \geq \{V_N(f), V_N(g)\} \\ &\Rightarrow V_N(g) \geq V_N(f) \end{aligned}$$

Hence  $V_N(f) = V_N(g)$ .

We can deal with the other case also in a similar way.

**Theorem 3.10 :** Let  $N$  be a VOGMR of  $\tilde{K}$ . Then  $K_N = \{f \in \tilde{K} \mid V_N(0)\}$  is a SOGMR of  $\tilde{K}$ .

Proof :

Let  $f, g \in K_N$  and  $\delta \in \Gamma$ .

So,  $V_N(f) = V_N(0)$  and  $V_N(g) = V_N(0)$ .

Now,

$$1. V_N(f - g) \geq \{V_N(f), V_N(g)\} = V_N(0)$$

$$2. V_N(f \delta g) \geq \{V_N(f), V_N(g)\} = V_N(0)$$

From 1 and 2, it is clear that  $f - g \in K_N, f \delta g \in K_N$ .

3. For every  $f, g \in K_N$  which contains an OGNR  $\tilde{K}$  implies  $K_N$  possess partial ordering. Thus is a SOGMR of  $\tilde{K}$ .

**Theorem 3.11 :** Let  $N = (t_N, f_N)$  and  $M = (t_M, f_M)$ , be two VOGMRs of  $\tilde{K}$ .

Then  $N \cap M$  is a VOGMR of  $\tilde{K}$ .

Proof: Let  $N = (t_N, f_N)$  and  $M = (t_M, f_M)$  be two VOGMRs of  $\tilde{K}$ . Then

$$\begin{aligned} t_{N \cap M}(f - g) &= \{t_N(f - g), t_M(f - g)\} \\ &\geq \\ &\{\{t_N(f), t_N(g)\}, \{t_M(f), t_M(g)\}\} \\ &= \min\{\{t_N(f), t_M(f)\}, \{t_N(g), t_M(g)\}\} \\ &= \{t_{N \cap M}(f), t_{N \cap M}(g)\} \text{ and } \\ 1 - f_{N \cap M}(f - g) &= \{1 - f_N(f - g), 1 - f_M(f - g)\} \\ &\geq \{\{1 - f_N(f), 1 - f_N(g)\}, \{1 - f_M(f), 1 - f_M(g)\}\} \\ &= \min\{\{1 - f_N(f), 1 - f_M(f)\}, \{1 - f_N(g), 1 - f_M(g)\}\} \\ &= \{1 - f_{N \cap M}(f), 1 - f_{N \cap M}(g)\} \end{aligned}$$

$$\begin{aligned} t_{N \cap M}(f \delta g) &= \{t_N(f \delta g), t_M(f \delta g)\} \\ &\geq \\ &\{\{t_N(f), t_N(g)\}, \{t_M(f), t_M(g)\}\} \\ &= \min\{\{t_N(f), t_M(f)\}, \{t_N(g), t_M(g)\}\} \\ &= \{t_{N \cap M}(f), t_{N \cap M}(g)\} \text{ and } \end{aligned}$$

$$\begin{aligned} 1 - f_{N \cap M}(f \delta g) &= \{1 - f_N(f \delta g), 1 - f_M(f \delta g)\} \\ &\geq \{\{1 - f_N(f), 1 - f_N(g)\}, \{1 - f_M(f), 1 - f_M(g)\}\} \end{aligned}$$

$$f_M(f)), \{1 - f_N(g), 1 - f_M(g)\} \\ = \{1 - f_{N \cap M}(f), 1 - f_{N \cap M}(g)\}$$

Now,

If  $f \leq g$  then  $t_N(f) \geq t_N(g)$  and  $t_M(f) \geq t_M(g)$

$$t_{N \cap M}(f) = \{t_N(f), t_M(f)\} \\ \geq \{t_N(g), t_M(g)\} \\ = t_{N \cap M}(g)$$

Therefore  $t_{N \cap M}(f) \geq t_{N \cap M}(g)$

And

$$1 - f_{N \cap M}(f) = \{1 - f_N(f), 1 - f_M(f)\} \\ \geq \{1 - f_N(g), 1 - f_M(g)\} \\ = 1 - f_{N \cap M}(g)$$

Therefore  $1 - f_{N \cap M}(f) \geq 1 - f_{N \cap M}(g)$

Hence  $N \cap M$  is a *VOG NR* of  $\tilde{K}$ .

#### IV. CONCLUSION

Conclusion: In this paper, we inspected the idea of *VOG NR*. We established one-one correspondence between *VOG NR* and crisp *OG NR*. We showed that the intersection of two *VOG NRs* is also a *VOG NR*.

#### V. ACKNOWLEDGMENT

The authors are grateful to Prof. K.L.N. Swamy and Prof. I.B Ramabhadra Sarma for their valuable suggestions and discussions on this work.

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